KeyWorld: Extracting Keywords from a Document as a Small World

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Abstract. The small world topology is known widespread in biological, social and man-made systems. This paper shows that the small world structure also exists in documents, such as papers. A document is represented by a network; the nodes represent terms, and the edges represent the co-occurrence of terms. This network is shown to have the characteristics of being small world, i.e., highly clustered and short path length. Based on the topology, we develop an indexing system called *KeyWorld*, which extract important terms by measuring their contribution to the graph being small world.

1 Introduction

Graphs that occur in many biological, social and man-made systems are often neither completely regular nor completely random, but have instead a "small world" topology in which nodes are highly clustered yet the path length between them is small [12][10]. For instance, if you are introduced to someone at a party in a small world, you can usually find a short chain of mutual acquaintances that connects you together. In the 1960s, Stanley Milgram's pioneering work on the small world problem showed that any two randomly chosen individuals in the United States are linked by a chain of six or fewer first-name acquaintances, known as "six degrees of separation" [6]. Watts and Strogatz have shown that a social graph (the collaboration graph of actors in feature films), a biological graph (the neural network of the nematode worm *C. elegans*), and a man-made graph (the electrical power grid of the western United States) all have a small world topology [12][11]. World Wide Web also forms a small world network [2].

In the context of document indexing, an innovative algorithm called *KeyGraph* [7] is developed, which utilizes the structure of the document. A document is represented as a graph, each node corresponds to a term[1], and each edge corresponds to the co-occurrence of terms. Based on the segmentation of this graph into clusters, *KeyGraph* finds keywords by selecting the term which co-occurs in multiple clusters. Recently, *KeyGraph* has been applied to several domains,

[1] A term is a word or a word sequence.

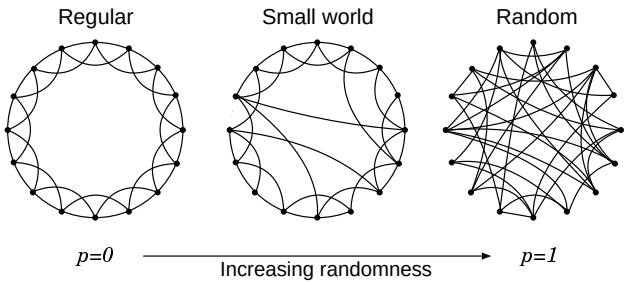

Fig. 1. Random rewiring of a regular ring lattice.

from earthquake sequences [8] to register transaction data of retail stores, and showed remarkable versatility.

In this paper, inspired by both small world phenomenon and *KeyGraph*, we develop a new algorithm, called *KeyWorld*, to find important terms. We show at first the graph derived from a document has the small world characteristics. To extract important terms, we find those terms which contribute to the world being small. The contribution is quantitatively measured by the difference of "small-worldliness" with and without the term.

The rest of the paper is organized as follows. In the following section, we first detail the small world topology, and show that some documents actually have small world characteristics. Then we explain how to extract the important terms in Section 3. We evaluate *KeyWorld* and suggest further improvements in Section 4. Finally, we discuss future works and conclude this paper.

2 Term Co-occurrence Graph and Small World

2.1 Small-worldliness

We treat an *undirected*, *unweighted*, *simple*, *sparse* and *connected* graph. (We expand to an *unconnected* graph in Section 3.) To formalize the notion of a small world, Watts and Strogatz define the clustering coefficient and the characteristic path length [12][11]:

- The *characteristic path length*, L, is the path length averaged over all pairs of nodes. The path length $d(i, j)$ is the number of edges in the shortest path between nodes i and j.
- The *clustering coefficient* is a measure of the cliqueness of the local neighbourhoods. For a node with k neighbours, then at most ${}_kC_2 = k(k-1)/2$ edges can exist between them. The clustering of a node is the fraction of these allowable edges that occur. The clustering coefficient, C is the average clustering over all the nodes in the graph.

Table 1. Characteristic path lengths L, clustering coefficients C and proximity ratios μ for graphs with a small world topology [10] (studied in [12])).

	L	L_{rand}	C	C_{rand}	μ
Film actor	3.65	2.99	0.79	0.00027	2396
Power grid	18.7	12.4	0.080	0.005	10.61
C. elegans	2.65	2.55	0.28	0.05	4.755

The graphs are defined as follows. For the film actors, two actors are joined by an edge if they have acted in a film together. For the power grid, nodes represent generators, transformers and substations, and edges represent high-voltage transmission lines between them. For *C. elegans*, an edge joins two neurons if they are connected by either a synapse or a gap junction.

Watts and Strogatz define a small world graph as one in which $L \geq L_{rand}$ (or $L \approx L_{rand}$) and $C \gg C_{rand}$ where L_{rand} and C_{rand} are the characteristic path length and clustering coefficient of a random graph with the same number of nodes and edges. They propose several models of graphs, one of which is called β-Graphs. Starting from a regular graph, they introduce disorder into the graph by randomly rewiring each edge with probability p as shown in Fig.1. If $p = 0$ then the graph is completely regular and ordered. If $p = 1$ then the graph is completely random and disordered. Intermediate values of p give graphs that are neither completely regular nor completely disordered. They are small worlds.

Walsh defines the proximity ratio

$$\mu = (C/L) \,/\, (C_{rand}/L_{rand}) \tag{1}$$

as the small-worldliness of the graph [10]. As p increases from 0, L drops sharply since a few long-range edges introduce short cuts into the graph. These short cuts have little effect on C. As a consequence the proximity ratio μ rises rapidly and the graph develops a small world topology. As p approaches 1, the neighbourhood clustering start to break down, and the short cuts no longer have a dramatic effect at linking up nodes. C and μ therefore drop, and the graph loses its small world topology. In Table 1, we can see μ is large in the graphs with a small world topology.

In short, small world networks are characterized by the distinctive combination of high clustering with short characteristic path length.

2.2 Term Co-occurrence Graph

A graph is constructed from a document as follows. We first preprocess the document by stemming and removing *stop words*, as in [9]. We apply n-gram to count phrase frequency. Then we regard the title of the document, each section title and each caption of figures and tables as a sentence, and exclude all the figures, tables, and references. We get a list of sentences, each of which consists of words (or phrases). In other words, we get a basket data where each item is a term, discarding the information of term orderings and document structures.

Table 2. Statistical data on proximity ratios μ for 57 graphs of papers in WWW9.

	L	L_{rand}	C	C_{rand}	μ
Max.	4.99	3.58	0.38	0.012	22.81
Ave.	5.36	—	0.33	—	15.31
Min.	8.13	2.94	0.31	0.027	4.20

We set $f_{thre} = 3$. We restrict attention to the giant connected component of the graph, which include 89% of the nodes on average. We exclude three papers, where the giant connected component covers less than 50% of the nodes. We don't show the L_{rand} and C_{rand} for the average case, because n and k differs dependent on the target paper. On average, $n = 275$ and $k = 5.04$.

Then we pick up *frequent terms* which appear over a user-given threshold, f_{thre} times, and fix them as nodes. For every pair of terms, we count the *co-occurrence* for every sentences, and add an edge if the Jaccard coefficient exceeds a threshold, J_{thre}[2]. The Jaccard coefficient is simply the number of sentences that contain both terms divided by the number of sentences that contain either terms. This idea is also used in constructing a referral network from WWW pages [5]. We assume the length of each edge is 1.

Table 2 is statistics of the small-worldliness of 57 graphs, each constructed from a technical paper that appeared at the 9th international World Wide Web conference (WWW9) 2000 [1]. From this result, we can conjecture these papers certainly have small world structures. However, depending on the paper, the small-worldliness varies.

One reason why the paper has a small world structure can be considered that the author may mention some concepts step by step (making the clustering of related terms), and then try to merge the concepts and build up new ideas (making a 'shortcut' of clusters). The author will keep in mind that the new idea is steadily connected to the fundamental concepts, but not redundantly. However, as we have seen, the small-worldliness varies from paper to paper. Certainly it depends on the subject, the aim, and the author's writing style of the paper.

3 Finding Important Terms

3.1 Shortcut and Contractor

Admitting that a document is a small world, how does it benefit us? We try here to estimate the importance of a term, and pick up important terms, though they are rare in the document, based on the small world structure. We consider 'important terms' as the terms which reflect the main topic, the author's idea, and the fundamental concepts of the document.

[2] In this paper, we set J_{thre} so that the number of neighbors, k, is around 4.5 on average.

First we introduce the notion of a *shortcut* and a *contractor*, following the definition in [11].

Definition 1. *The range $R(i,j)$ is the length of the shortest path between i and j in the* absence *of that edge. If $R(i,j) > 2$, then the edge (i,j) is called a* shortcut.

Applying the notion of "shortcuts" in terms of nodes, we can get the definition of "contractor."

Definition 2. *If two nodes u and w are both elements of the same neighbourhood $\Gamma(v)$, and the shortest path length between them that does not involve any edges adjacent with v is denoted $d_v(u,w) > 2$, then v is said to* contract *u and w, and v is called a* contractor.

In our first thought, if $d_v(u,w)$ is large, the corresponding term of contractor v might be interesting, because they bridge the distant notions which rarely appear together. However, such a node sometimes connects the nodes far from the center of the graph, i.e. the main topic of the document. Below we take into account the whole structure of the graph, calculating the contribution of a node to make the world small.

To treat the disconnected graph, we expand the definition of path length (though Watts restricts attention to the giant connected component of the graph).

Definition 3. *An* extended *path length $d'(i,j)$ of node i and j is defined as follows.*

$$d'(i,j) = \begin{cases} d(i,j), & \text{if } (i,j) \text{ are connected,} \\ w_{sum}, & \text{otherwise.} \end{cases} \tag{2}$$

where w_{sum} is a constant, the sum of the widths of all the disconnected subgraphs. $d(i,j)$ is a path length of the shortest path between i and j in a connected graph.

If some edges are added to the graph and some parts of the graph gets connected, $d'(i,j)$ will not increase, unless the length of an edge is negative. Thus $d'(i,j)$ is one of the upper bounds of the path length considering the edges will be added.

Definition 4. Extended characteristic path length *L' is an extended path length averaged over all pairs of nodes.*

Definition 5. *L'_v is an extended path length averaged over all pairs of nodes except node v. L'_{G_v} is the extended characteristic path length of the graph without node v.*

In other words, L'_v is the characteristic path length regarding the node v as a corridor (i.e., a set of edges). For example, if v is neighboring u, w, and z, then $(u,w), (u,z), and (w,z)$ are considered to be linked. And L'_{G_v} is the extended characteristic path length assuming the corridor doesn't exist.

Table 3. Frequent terms in this paper.

Term	Frequency
term	39
small	36
world	35
graph	33
small world	27
node	26
document	25
length	20
important	19
paper	18

Table 4. Terms with 10 largest CB_v in this paper.

Term	CB_v	Frequency
small world	4.38	27
contribution	3.11	11
node	2.98	26
list	2.24	8
author	1.36	7
table	1.10	8
important term	0.80	11
show	0.72	6
structure	0.44	7
KeyWorld	0.44	10

Definition 6. *The* contribution, CB_v, *of the node* v *to make the world small is defined as follows.*

$$CB_v = L'_{G_v} - L'_v \tag{3}$$

We don't pay attention to the clustering coefficient, because adding or eliminating one node affects the clustering coefficient little.

If node v with large CB_v is absent in the graph, the graph gets very large. In the context of documents, the topics are divided. We assume such a term help merge the structure of the document, thus important.

3.2 Example

We show the example experimented on this paper, i.e., the one you are reading now[3]. Table 3 shows the frequent terms and Table 4 shows the important terms measured by CB_v. Comparing two tables, the list of important terms includes

[3] We ignore the effect of *self-reference*; it's sufficiently small.

Table 5. Pairs of Terms with 10 Largest CB_e.

Pair	CB_e
node – contribution	2.97
list – table	1.47
contribution – important term	1.20
table – show	1.10
contribution – structure	0.87
KeyWorld – list	0.87
important term – develop	0.79
network – show	0.72
contribution – make	0.47
author – idea	0.47

the author's idea, e.g., "important term" and "KeyGraph," as well as the important basic concept, e.g., "structure," although they are not frequently appeared. However the list of frequent terms simply show the components of the papers, and are not of interest.

We can also measure the contribution of an edge, CB_e, to make the world small, defined similarly as CB_v. However, if we look at the pairs of terms in Table 5, it is hard to understand what they suggest. There are numbers of relations between two terms, so we cannot imagine the relation of the pairs right away.

Lastly, Fig. 2 shows the graphical visualization of the world of this paper. (Only the giant connected component of the graph is shown, though other parts of the graph is also used for calculation.) We can easily point out the terms without which the world will be separated, say "small world" and "comtribution".

4 Evaluation and Improvements

This section describes an evaluation of *KeyWorld* as an indexing system. *KeyWorld* is not merely an indexing system but it provides an understandable graphical representation of the document. However, we restrict attention here to the performance of *KeyWorld* as an indexing tool to compare it with existing indexing techniques such as *tf* and *tfidf*. The *tf* measures simply term frequency. The *tfidf* measure is obtained by using the product of the term frequency and the inverse document frequency[9][4].

When an author writes a paper, he/she annotates keywords to his/her paper by selecting the category of the paper (e.g. "text mining"), utilized algorithms (e.g. "small world"), or the proposed method (e.g. "KeyWorld"). The choice depends on the author's criteria. In our definition, a keyword is an important term in the document, which reflects the main topic, the author's idea, and the fundamental concepts of the document. For example, considering this paper,

[4] We use $\log N/n_v$ as *idf*, where N is the number of document collection, and n_v is the number of document which includes term v.

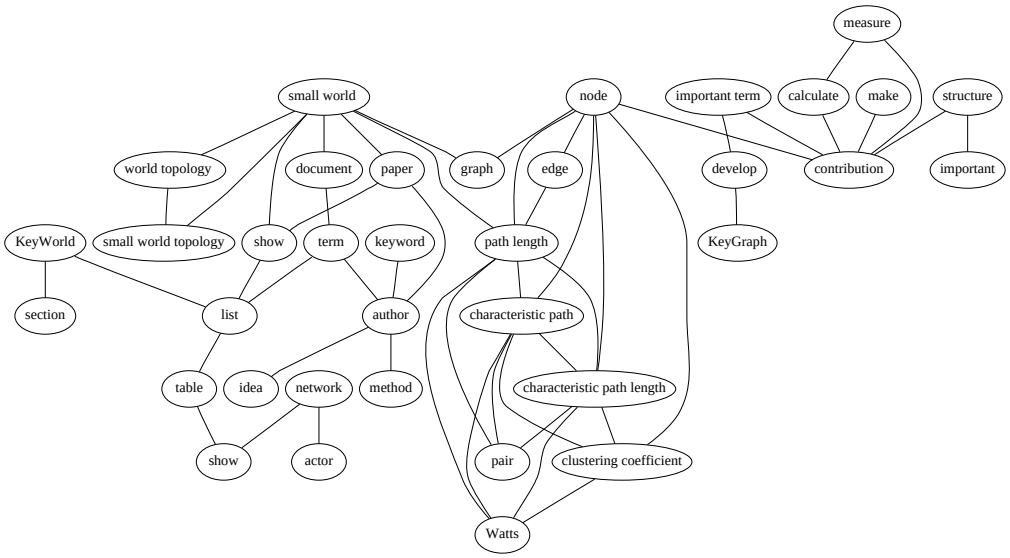

Fig. 2. Small world of this paper.

we think "small world," "document," "contribution," "important term," "path length," and "KeyWorld" are keywords, and "node," "make," and "text mining" are not keywords because they are too trivial or too broad, or do not occur in this document.

In the experimentation, we asked the authors of 20 technical papers in the artificial intelligence field to judge whether some terms in their papers are keywords or not by a questionnaire. For each document, we first get top 15 weighted terms by *tf*, *tfidf*[5], *KeyGraph*, and *KeyWorld*, i.e. the four lists of 15 terms. (We denote the list by method a as $list_a$.) We merge the four lists and shuffle the terms. Then we ask the author whether each term is a keyword or not after explaining the definition of keywords. Counting the number of authorized terms, we can get the precision of method a as follows.

$$precision_a = \frac{\text{Number of authorized terms in } list_a}{\text{Number of terms in } list_a} \tag{4}$$

Next, from the shuffled list of all terms[6], the authors are told to pick 5 (or more) terms as indispensable terms which they think are essential to the document, and cover the most important concepts of the paper. We calculate

[5] As a corpus, we used 166 papers in Journal of Artificial Intelligence Research, from Vol.1 in 1993 to Vol.14 in 2001.

[6] If the author remembers the other terms, he/she is permitted to add them to the list.

Table 6. Precision and Coverage

	tf	*KeyWorld*	*tfidf*	*KeyWorld+idf*
precision	0.53	0.49	0.55	0.71
coverage	0.48	0.50	0.62	0.68

Table 7. Terms with 10 largest $CB_v \times idf_v$ in this paper.

Term	$CB_v \times idf_v$	Frequency
small world	4.57	27
important term	3.82	11
co-occurrence	1.89	4
KeyWorld	1.58	10
short cut	1.56	4
actor	0.89	5
shortest path	0.66	4
sentence	0.66	4
document	0.66	23
path length	0.59	17

the coverage of method a as follows.

$$coverage_a = \frac{\text{Number of indispensable terms in } list_a}{\text{Number of indispensable terms}} \tag{5}$$

The results are shown in Table 6. The performance of *KeyWorld* is not good enough. The precision and coverage are almost equal to *tf*. However, we feel that the term list by *KeyWorld* includes very important terms as well as very dull words, e.g. "show" or "table" in Table 4. To sieve out these dull terms, we develop an improved weighting method, which annotates term v with the weight

$$CB_v \times idf_v, \tag{6}$$

where idf_v is an *idf* measure for term v. The improved results are also shown in Table 6. Both the precision and coverage are now far better than *tfidf*. Table 7 shows the top 10 terms by *KeyWorld* with *idf* factor for this paper.

In summary, *KeyWorld* can often find important terms, however, it also detect less important terms. By incorporating with the *idf* measure, *KeyWorld* can be a very good indexing tool.

5 Discussion

The small world phenomenon was inaugurated as an area of experimental study in the social sciences by Stanley Milgram in the 1960's. Since then, numerous

studies have been done for network analysis. The importance of weak ties, which is a short cut between clusters of people, was mentioned 30 years ago [4].

The measure of contribution is similar to "*centrality*" in the context of social network study. Centrality can be measured in a number of ways [3]. Considering an actors' social network, the simplest is to count the number of others with whom an actor maintains relations. The actor with the most connections, i.e., the highest *degree*, is most central. Another measure is *closeness*, which calculates the distance from each person in the network to each other person based on the connections among all members of the network. Central actors are closer to all others than are other actors. A third measure is *betweenness* which examines the extent to which an actor is situated between others in the network, i.e., the extent to which information must pass through them to get to others, and thus the extent to which they will be exposed to information circulating in the network. However, our measure of *contribution* has a characteristic in that it calculates the difference of the closeness of all nodes with and without a certain node. It measures a node's contribution to the whole structure by temporarily eliminating the node.

6 Conclusion

Watts mentions in [11] the possible applications of small world research, including "the train of thought followed in a conversation or succession of ideas leading to a scientific breakthrough." In this paper, we have focused on the papers rather than conversation or succession of ideas. The future direction of our research is to treat *directed* or *weighted* graph for finer analyses of the document.

We expect our approach is effective not only to document indexing, but also to other graphical representations. To find out structurally important parts may bring us deeper understandings of the graph, new perspectives, and chances to utilize it. We are interested in a big structural change caused by a small change of the graph. A change, which makes the world very small, may sometimes be very important.

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